



# Serendipity-based Points-of-Interest Navigation

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Traditional venue and tour recommendation systems do not necessarily provide a *diverse* set of recommendations and leave little room for *serendipity*. In this article, we design MPG, a Mobile Personal Guide that recommends: (i) a set of diverse yet surprisingly interesting venues that are aligned to user preferences and (ii) a set of routes, constructed from the recommended venues. We also introduce EPUI, an Experimental Platform for Urban Informatics. Our comparison with the state-of-the-art schemes indicates that MPG is capable of providing high-quality venues and route recommendations while incorporating seamlessly both the notion of diversity and that of serendipity.

CCS Concepts: • **Information systems** → **Information retrieval diversity**; **Top-k retrieval in databases**; **Mobile information processing systems**; • **Human-centered computing** → **Ubiquitous and mobile computing**;

Additional Key Words and Phrases: POIs recommendation, relevance, diversity, serendipity

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## 1 INTRODUCTION

The rapid developments in mobile computing lead to the transformation of traditional Yellow pages to mobile applications that are conveniently reachable, up-to-date, localized, and personalized,

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connected to the surroundings, and versatile in many other ways. Platforms such as Yelp and Foursquare allow their users to generate multimedia content (e.g., text, image) and share their experiences with their peers.

Many systems have been developed and built on top of these platforms for recommending specific venues or Points of Interest (POIs) to be visited by users, i.e., *digital travel guides*. Given that this digitization results in a richer and up-to-date content, the possibilities for providing flexible, personalized guides are huge. Personalized tour systems have also appeared in the literature (e.g., [28]) that take into consideration spatiotemporal constraints, users' interests, and so on. Nevertheless, many of the approaches to date are monolithic and myopic to user preferences, returning generic recommendations where every location is treated equally (e.g., References [6, 16, 20, 38, 58]).

*Example:* The following scenario best illustrates how a well-designed digital travel guide will help travelers. Pam is a businesswoman who visits Pittsburgh for the first time on a business trip. After finishing all her business meetings in the morning, she wants to have a cup of coffee before finding a restaurant for lunch, so she turns to her smartphone to quickly find 100 coffee shops and restaurants near her via a digital travel guide. Since the digital travel guide already knows her coffee preference, via a *personalized* profile, it is able to recommend precisely the nearest Starbucks, as Pam likes Starbucks' cappuccino. As she finishes her coffee, Pam wants to proceed with the lunch, so she queries the digital travel guide for the top-two restaurants through a user-friendly query interface. This time the digital travel guide provides her with two *diverse* restaurants, Souvlaki and Pizza Hut, each from one of her two favorite food types, Greek and Pizza, respectively. After lunch, Pam wanted to spend some relaxing time and visit some of the interesting venues of Pittsburgh, so she again turns to her digital travel guide, this time for a recommendation of four interesting venues. The digital travel guide knows Pam is a history and science enthusiast and she loves to visit museums, so it first recommends two great museums, namely the Heinz History Center and the Carnegie Science Center, which are about the same distance from her current location. It also recommends for the third spot a smaller museum at Fort Pitt, established by the British between 1759 and 1761 and later developed as Pittsburgh. However, for the fourth spot on the recommendation list, instead of recommending another museum, the digital travel guide *surprises* her with the recommendation of the Nationality Rooms of the Cathedral of Learning,<sup>1</sup> which is something that Pam has never heard of but instantly recognized as a *must-go* venue after reading their descriptions.

Clearly, one of the key components of such a digital travel guide is its venue recommendation algorithm. A common approach to venue recommendation among prior works—personalized or not—is the ranking of venues based on some quality features (e.g., References [21, 28, 40, 51, 55]). Consequently, the top-*k* venues are returned. There are two major drawbacks to this approach. First, it does not allow for a *diverse* set of recommendations, because similar venues tend to have a similar ranking, and thus the top venues will all be similar to each other with high probability. Second, these systems are overwhelmingly focused on optimizing an *efficiency objective*, such as minimizing the distance covered and maximizing the benefit obtained from the route as captured by a measure of venue quality (e.g., References [28, 40, 55]). It is only in recent years that efforts have been made to consider objectives that go beyond the pure efficiency (e.g., References [21, 51]), but they are still in a nascent stage.

The first drawback at a high level translates to a poor recommendation, since the *effective* choice of the user is reduced, given that many of the recommended venues will offer similar experiences.

<sup>1</sup>The Nationality Rooms are a collection of 31 classrooms in the University of Pittsburgh's main building Cathedral of Learning depicting and donated by the national and ethnic groups that helped build the city of Pittsburgh. [2].

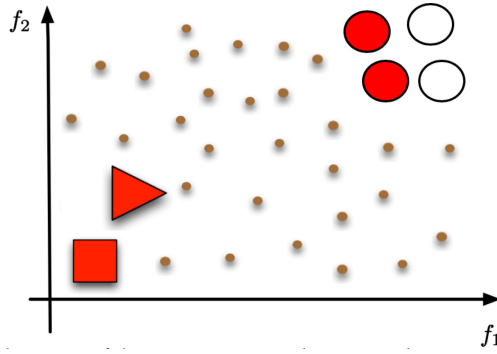


Fig. 1. MPG provides a set of diverse recommendations without sacrificing the quality.

The second drawback leads to recommendations that do not capture the great and livable aspect of a city, as the features that contribute to capturing a livable environment are missing in these systems. That is, traditional recommendation systems do not encourage users to step outside their comfort zones and discover unexpected but interesting venues. The objective in this article is to design a *Mobile Personal Guide* (MPG) that addresses both drawbacks of the existing systems and delivers an interactive response (i.e., sub-second) for each query to guarantee smooth user interactions.

**MPG Overview.** To address the first drawback of the common approach, MPG takes into consideration the user's preferences and provides a set of venues that satisfy the imposed constraints with maximized diversity. The diversity (as formally defined later in Section 3) is essentially a measure of dissimilarity of the venues based on external attributes. Simply put, MPG outputs a set of high-quality yet diverse venues. To illustrate this objective, let us consider again our example scenario above, where 35 venues satisfy Pam's preferences, depicted in Figure 1. Assume that Pam only has time to visit 4 of them, as in our example scenario above. The venues represented by the large circles correspond to the top-4 venues ranked; for instance, based on their popularity (i.e., top-4 venues with highest popularity). The venues represented by the triangle and the square are ranked fifth and sixth, respectively. The rest of the venues are ranked lower and are represented by the brown dots. The space corresponds to two external features ( $f_1$ ,  $f_2$ ) that define the similarity of a pair of venues. In particular, the top-4 venues are very close in this space and hence are similar (or in other words, they have low diversity in the space defined by  $f_1$  and  $f_2$ ). A system that does not consider the diversity of the recommended venues would most certainly choose these venues as output. However, MPG allows the user to explore the available venues in this latent space—without sacrificing the quality of the recommendations—and so it would return to the user the top-2 venues, as well as the fifth and sixth, ranked venues (the venues with a red fill). As we can see, this set is more widespread in this latent space as compared to the top-4 venues (whether these are restaurants or museums). Furthermore, since it is impossible for any recommendation system to guarantee 100% user satisfaction, it is also important to construct a set of recommendations with broad coverage of the initial candidate set of venues (i.e., recommend venues that represent a large portion of the candidate venues). This will help the system to increase the chance of recommending venues that are interesting to the user and provide the user with the possibility to zoom into venues that they are interested in and discover more similar venues if they prefer.

In a nutshell, our approach consists of the following basic steps. First, we begin with assigning intensity value  $I_p^v$  to venue  $v$  based on its *popularity*. We also assign a distance intensity value  $I_{d,q}^v$ , which captures the distance between the current location  $q$  of the mobile user and venue  $v$ .

By combining  $I_p^v$  and  $I_{d,q}^v$ , we obtained a composite intensity value,  $I_{p,d}^v$ . We further tune these intensity values based on the preferences of user  $u$  obtaining  $I_{p,d,u}^v$ , which forms our composite intensity value space  $I_k^v$ . Finally,  $I_k^v$  along with a vector  $\mathbf{f}_v$  that represents venue  $v$  in the latent space (i.e., external attributes) form the input to our modified PrefDiv (*Preferential Diversity*) algorithm [23], whose output is the required recommendations. One of the advantages of PrefDiv is that it offers the mobile user the ability to adjust the balance between relevance and diversity in the returned results.

To address the second drawback of the common approach, MPG introduces the important concept of serendipity, which has been identified as a characteristic that can significantly improve the quality of experience that a city-dweller has [41]. We define serendipity as the recommendation of items that are relevant to a user but unexpected and happily surprising. Recent studies (e.g., [31, 39]) have shown that recommending items that are relevant while unexpected is an essential factor in increasing user satisfaction and prevent filter bubbles.

It is worth pointing out that serendipity is a very different concept from diversity, which constitutes ex-post process and can be combined with serendipity. Specifically, diversity in the context of the recommendation systems can generally be understood as a property that applies to a set of recommended items that measures how dissimilar items are to each other in a set, which involves measuring the average pairwise dissimilarity of items through some dissimilarity metrics. Even though a consensus definition for serendipity in the context of the recommendation system has not yet been formed, based on previous studies (e.g., References [3, 46, 61]), relevance and unexpectedness have been identified as the two most essential elements in defining the serendipity in the recommendation context. In particular, the relevance refers to the quantitative measure of the benefit of recommending an item, and the unexpectedness requires the recommended items to be unexpected by the user and is typically achieved through randomness and non-determinism algorithms. Unlike diversity, serendipity does not prevent similar items to be recommended as long as the recommended items are relevant to and unexpected by the user (e.g., the recommendation of two historical museums to a history lover where he/she is not even aware that the second museum exists).

In other words, diversity and serendipity are complementary to each other. To better illustrate the difference between diversity and serendipity, let us consider a recommendation request for a set of  $k$  items that are both relevant and diverse from a database with  $N$  items. Typically, the number of mutual dissimilar items  $C$  in the database that are relevant is much larger than the requested  $k$  items (i.e.,  $k < C \leq N$ ). A typical recommendation system will employ some method to recommend a subset of  $k$  item from  $C$  that has the best tradeoff between relevance and diversity, such as top- $k$ . In this scenario, adding serendipity means picking the  $k$  recommendation from these  $C$  relevant yet diverse items in a non-deterministic fashion to fulfill the unexpectedness. Clearly, from this example, one can tell that serendipity is a stand-alone concept that can be applied in conjunction with the diversity and relevance.

MPG incorporates serendipity in two layers, both of which explore *randomness*. At the first layer, serendipity is achieved through the recommendations of venues based on PrefDiv. We develop a probability-based variant of PrefDiv, namely, *Probabilistic Preferential Diversity* (pPrefDiv), which incorporates the necessary serendipity for a surprisingly interesting recommendation of venues. The second layer of serendipity is achieved through the recommendation of routes. Specifically, we utilize random walks to generate a set of initial routes. The randomness of this process essentially captures the desired serendipity, since the venues to be included in the route are not chosen in a way that optimizes a pre-defined objective. Last, the Pareto front is deployed to pick final recommendations that show high quality with respect to both diversity and serendipity.

**Contributions.** In summary, this article's contributions are as follows:

- We introduce a new mobile service, coined MPG, which is capable of generating venue recommendations that are not only *popular* and *relevant* to user's preference but are also *diverse*. Our method ranks venues based on user preferences, the distance to the venue, and the popularity of a venue based on check-in information, and achieves diversity with a novel semantic distance function.
- We formally introduce the notion of *serendipity*, and effectively integrate serendipity in MPG into both venue and route recommendation by means of randomness while still preserving the relevance and diversity aspects of recommendations. We describe in detail *Probabilistic Preferential Diversity* (pPrefDiv), which supports serendipity in venues, and formally introduce a random-walk-based routing method that achieves the serendipity in route recommendation. Specifically, we propose four novel schemes for achieving serendipity in route recommendations, namely *PrefDiv+Random Walk*, *pPrefDiv+Random Walk*, *pPrefDiv+ShortestDistance*, and *pPrefDiv+HighestRelevance*. We also propose a new metric to measure their degree of serendipity, which is the deviation of a route from the most anticipated, non-deterministic, top route.
- We present as a proof-of-concept the design and implementation of two prototype systems: (i) MPG for Android devices; and (ii) EPUI, our Experimental Platform for Urban Informatics that supports the personalized venue and route recommendation in an interactive manner. EPUI supports a number of state-of-the-art approaches for the venue and tour recommendations and enables their comparison by presenting the recommended venues and tours visually on a street map as well as displaying evaluation metrics through summary dashboards. EPUI's implementation is flexible and allows for different diversity and indexing schemes to be incorporated as well as new recommendation algorithms to be uploaded. Hence, EPUI can be used by the broader research community to facilitate the evaluation of alternative POIs recommendations and route construction algorithms.
- We experimentally compare our proposed solutions to other state-of-the-art alternatives (i.e., K-Meroids, DisC Diversity, and Random for venue recommendations and two deterministic baseline schemes for serendipity-based route recommendations) using three datasets (i.e., NYC, San Francisco, and Pittsburgh). In our comparisons, in addition to the standard metrics (e.g., coverage, intensity value), we used our proposed metric that capture the degree of serendipity in route recommendation. Our extensive experiments verify the effectiveness of our proposed solutions, showing that MPG can successfully increase coverage of the result-set compared to other alternatives, achieve a significantly better *Relevance-Diversity* tradeoff than other methods, and offer high degree of serendipity. They also verify its ability to support interactive response time.

The rest of the article is organized as follows: In the next section, we review related work. In Section 3, we formally define our problem and describe the basic components of the MPG design. We introduce the serendipity venue and route recommendation algorithms in Sections 4. The MPG prototype and EPUI experimental platform are presented in Section 5. Our thorough experimental evaluation and its findings are reported in Section 6. Section 7 concludes our work and briefly describes our future directions.

## 2 RELATED WORK

In this section, we discuss existing works that are strongly related to our own. In particular, we will present studies related to trip planning as well as methods for query personalization.



## 2.1 Trip Planning and Spatial Recommendations

During the past few years, there has been a large volume of studies that focus on methods for personalized location/POI recommendations to social-network users [8, 47, 57]. The majority of existing work utilizes collaborative-filtering techniques [57] or geometric embeddings [8], or they even incorporate features present in the users' social network [47] to associate every venue with a score, which is representative of the probability of a user enjoying (or liking) a particular venue. The aforementioned studies consider and evaluate each venue independently. Hence, motivated by this monolithic view of these methods, recent work has focused on recommending *tours* of locations. For instance, De Choudhury et al. [16] focus on segmenting streams of spatiotemporally tagged photos into paths and then assembling these paths into itineraries. Similar studies by Kurashima et al. [40] and Yoon et al. [58] are based on geotagged content from photo-sharing media (e.g., photo streams, GPS trajectories) to recommend future travel paths. However, these approaches come with their drawbacks. For example, to be applicable, the presence of training sequences of spatiotemporally tagged photographs (or other similar traces) is required. These approaches cannot handle multiple types of venues that cater to different user needs. The same is true for interactive systems [6, 20, 38], which iteratively personalize or improve a tour based on user feedback.

The support for multiple types of venues is considered by Ardissono et al. [5], where the user *manually* selects a venue from each desired type, and then a tour traversing the selected venues is proposed. More recently, Gionis et al. [28] developed a system based on dynamic programming algorithms, which provides spatially constrained tours based on user preferences of the category of venues. Other spatial recommendation approaches focus on reconstructing and recommending routes based on existing location trajectories (e.g., References [11, 55]).

Existing works (e.g., References [29, 42, 43, 57]) that employed a collaborative filtering-based approach for venue recommendation identify a set of similar users based on user previous interactions (e.g., feedbacks, ratings) with venues and then predict a user's rating for a venue that they have not rated based on the observed ratings of the venue of similar users and the properties of the venue. In recent years, one commonly used algorithm for collaborative filtering-based recommender systems is matrix factorization (e.g., References [29, 42]) that decomposes a user-item rating matrix into a product of two-factor matrices  $U$  and  $I$ . The prior represents the relation between some latent factors and the users, and the latter represents the relation between latent factors and the items. Such decomposition essentially maps both users and items to a joint latent factor space of dimensionality  $f$ , such that recommendations are derived based on the user-item interactions modeled as inner products in that space. Matrix factorization can also be generalized to accommodate more information (e.g., contextual) going beyond just the information of users and items. Such a generalization of matrix factorization is called tensor factorization [32], which allows for more flexible and generic integration of multi-dimensional data. Instead of the traditional two-dimensional user-item matrix, tensor factorization integrates additional information by modeling the data as an  $N$ -dimensional tensor (e.g., User-Item-Context).

Recently, Lu et al. [43] has proposed methods that aim to promote serendipity in matrix factorization-based recommender systems. However, these methods use "serendipity" as a way to recommend unpopular items that are relevant to a user's preference and do not capture the non-deterministic, unexpected characteristic of true serendipity. Although matrix- or tensor factorization-based techniques provide a high degree of accuracy on the estimation of the preferences between users and items, they do not provide any guarantees for diversity or serendipity of the results. Furthermore, matrix- or tensor factorization-based recommender systems suffer from cold start-related problems (e.g., when a new user or item has been added to the system) as well

as low scalability due to their superlinear time and space complexity [52]. Therefore, they are not suitable for interactive exploratory range queries in digital travel guides that demand sub-second latency.

Other recent works (e.g., References [7, 60]) have studied the problem of recommending a trip with a diverse set of venues by employing taxonomies or categorical hierarchies to diversify the venues. Their approaches only capture the coarse-grained difference between venues, and, thus, they are unable to distinguish between venues that are within the same category. As such, for a top-4 query that recommends four venues from two venue categories coffee shop and gym, they could recommend {Starbucks 1, Starbucks 2, 24 Hour Fitness A, and 24 Hour Fitness B} rather than the more diverse recommendation of {Starbucks 1, Costa Coffee, 24 Hour Fitness A, and Anytime Fitness}.

Existing work addresses the problem of finding spatially diverse routes in two different ways. Lu et al. [44] proposed to integrate the output of several different location recommender systems to form the top- $k$  recommendations with two aggregation strategies: (i) to use the scaled score produced by each recommender systems and (ii) to rely on the ranked position of a location in each recommender system's recommendation and assign higher scores to the top locations. Both these aggregation strategies have their drawbacks. The score-based approach requires a proper scaling between the scores produced by different recommendation algorithms, which is typically a challenging task, and the position-based approach is less effective when the overlap between the recommendations produced by different algorithms is small. Furthermore, it does not provide explicitly guarantee on the diversity of the final recommendations. Xu et al. [56] propose to generate the desired subset of spatially diverse routes from a large set of relevant but semantically similar routes (i.e., routes that pass through POIs of the same categories given by the user). Since this approach only focuses on finding routes that are diverse with each other based on the spatial distance between the two routes, it does not take into consideration the semantic diversity between POIs or serendipity. To the best of our knowledge, there is no study to date that considers the venue coverage, semantic diversity (in a latent space) in combination with serendipity when it comes to recommendations.

## 2.2 Query Personalization

**Relevance.** The combination of user preferences and result diversification techniques, which yield the Relevance rankings, have been previously proposed to deal with the problem of information overload (i.e., avoid overwhelming users with a large volume of irrelevant results). Ranking techniques are comprehensively surveyed in Reference [53].

Mostly these techniques can be distinguished based on the type of preferences they support for filtering and ordering data. These techniques primarily handle only one type of preference, either *quantitative* or *qualitative*. However, each preference type has its own advantages and disadvantages. Hybrid schemes that support both qualitative and quantitative preferences have been proposed in an attempt to exploit the advantages of both types of preferences while eliminating their disadvantages [27, 37]. In this work, our proposed algorithms can work with any existing relevance ranking model that returns a set of sorted tuples/objects along with their scores/intensity values.

More recently, in Reference [10], the authors studied the problem of producing rankings while preserving a given set of fairness constraints. In particular, the proposed algorithm takes as input, a utility function, a collection of sensitive attributes (e.g., gender, race) of each item, and a collection of fairness constraints that bound the number of items with each sensitive attribute that are allowed to appear in the final results. It outputs a ranking that maximizes the relevance with respect to the given utility function while respecting the fairness constraints.

**Diversity.** In recent years, result diversification has been extensively studied in many different contexts (e.g., References [18, 33–36]), and with various definitions such as similarity, semantic coverage [4], and novelty [15]. In our work, we focus on the similarity definition and use MaxMin and MaxSum, which are two widely used diversification models, as baselines.

The goal of these two diversification models is to select a subset  $S$  from the object space  $R$ , so that the minimum or the total pairwise distances of objects in  $S$  is maximized. Recently, a number of variations of the MaxMin and MaxSum diversification models have also been proposed (e.g., References [17, 48]) to address the problem of diversifying continuous data. Formally, MaxMin and MaxSum are defined as follows:

*Definition 1.* MaxMin generates a subset of  $R$  with the maximum  $f = \min_{p_i, p_j \in S} dt(p_i, p_j)$ , where  $dt$  is some distance function  $p_i \neq p_j$  for all subsets with the same size.

*Definition 2.* MaxSum generates a subset of  $R$  with the maximum  $f = \sum_{o_i, o_j \in S} dt(o_i, o_j)$ , where  $dt$  is some distance function  $o_i \neq o_j$  for all subsets with the same size.

*DisC Diversity* (or *DisC* for short) [18] is the most recently proposed diversity framework and solves the diversification problem from a different perspective. In DisC Diversity, the number of retrieved diverse results is not an input parameter. Instead, users define the desired degree of diversification in terms of a tuning parameter  $r$  (radius). DisC Diversity considers two objects  $o_i$  and  $o_j$  in the query result  $R$  to be similar objects if the distance between  $o_i$  and  $o_j$  is less than or equal to a tuning parameter  $r$  (radius). It selects the representative subset  $S \subseteq R$  according to the following conditions: (i) For any objects in  $R$ , there should be at least one similar object in  $S$ , and (ii) all objects in  $S$  should be dissimilar to each other. These two conditions ensure both the coverage and the dissimilarity property of a diverse result set.

The key differences between PrefDiv algorithms used by the MPG and DisC Diversity are as follows: (i) PrefDiv algorithms follow the Top- $k$  paradigm, which provides users with the option to specify the size of the final result set by assigning a value to parameter  $k$ , whereas DisC Diversity adjusts the size of the result set by changing its radius parameter  $r$ . (ii) The PrefDiv algorithms focus on both the *relevance* of the result set with respect to the users' preference and the *diversity* of the result set. DisC Diversity focuses mainly on the most diverse representative subset with two scenarios that only illustrate the possibility of using DisC Diversity to handle such relevance-aware diversity requests; however, they do not mention any specific strategies on how one can dynamically change the radius  $r$ .

Another way to generate a diverse, representative set of results is through clustering. One example of this would be *k-Medoids*, which is a well-known clustering algorithm that attempts to minimize the distance between points in a cluster and the center point (medoid element) of that cluster. The *k-Medoids* algorithm can be classified into two stages: In its first stage, it generates a set of  $k$  clusters  $C = \{c_1, c_2, \dots, c_k\}$  based on some distance function  $dt$ . In the second stage, one element from each cluster is selected to be part of the result set  $R$ . Several strategies for selecting an element from each cluster could be employed. For instance, one strategy is to choose the center point of each cluster, which is expected to deliver high diversity, and another strategy would be to choose the point that has the highest intensity value for each cluster. However, since there is no parameter that can be tuned either manually or automatically to balance the tradeoff between relevance and diversity, *k-Medoids* is unable to balance such a tradeoff in fine granularity.

**Multi-Criteria Objective Optimization.** Even though the goal of diversity is to avoid loss of potentially important data due to its low ranking, the result of diversification does not automatically imply relevance for the users. This was the underlying motivation for the top- $k$  diversification techniques, such as PrefDiv [23], Swap [59], the *Query Manifold (QM)* framework [62]. This was



also the motivation for the multi-objective optimization approaches in which the first objective is relevance and the second objective is dissimilarity [63]. As opposed to *PrefDiv*, *Swap*, and the multi-objective optimizations that recommend relevant and diverse data, *QM* recommends a set of relevant and diverse queries.

The difference between *PrefDiv* and *Swap* is that the latter seeks diversity through pairwise distances of items among the result-set and filters out items that contribute less to diversity. *Swap* ensures relevance by removing items that drop the relevance below a pre-defined threshold. In contrast, *PrefDiv* seeks diversity by eliminating similar items and ensures relevance by using a relevance-focused greedy algorithm that can reflect the user-specified relevance distribution.

The most widely known approach that is targeted directly at optimizing the tradeoff between diversity and relevance was introduced in Reference [9]. In this work, the authors have proposed the twin-objective function called *Maximal Marginal Relevance* (MMR), which combines both relevance and diversity aspects in a single comprehensive, objective function with a scaling factor  $\lambda$ . When  $\lambda = 1$ , the MMR function equals to a standard relevance ranking function, when  $\lambda = 0$  it computes a maximal diversity ranking. Compared to *PrefDiv*, MMR always requires to compute its objective function against the entire set of initial candidate items for each of its  $k$  representative items, whereas *PrefDiv* does not rely on a single comprehensive, objective function and in most cases only requires a very small number of comparisons for each of its  $k$  representative items. Recently, a new MMR function that integrates regret minimization was proposed to generate the relevance score [30]. This new score attempts to minimize the disappointment of users when they see  $k$  representative tuples rather than the whole database.

*Div-Astar* [50] is another multi-criteria objective optimization solution that is graph based, in which each node corresponds to one item in the original data. This diversity graph is sorted according to the relevance score, and an  $a^*$  algorithm is used to find the exact solution for diversifying top- $k$  results. That is, *Div-Astar* considers the problem as finding the optimal solution for the maximum weight independent set problem, which has been proven to be NP-hard.

Our proposed MPG system differs from all of the above works, as MPG leverages the capability of *pPrefDiv*, the nondeterministic version of *PrefDiv*, to provide venue recommendation that optimizes three important aspects of venue recommendation (i.e., relevance, diversity, and coverage), while delivering results that are unexpected by the user. Furthermore, MPG is capable of providing serendipity-based route recommendations with relevance and diversity in mind.

### 3 MPG DESIGN

In this section, we introduce the formal underpinnings of MPG and its core components (Figure 2). We begin by formally defining relevance and diversity that are central to our work.

#### 3.1 Relevance, Intensity, Diversity, Similarity, and Coverage

**Relevance.** We represent the degree or score of relevance of an item  $o$  to a user  $u$  by the *Preference Intensity Value* ( $I_u^o$ ).

*Definition 3.* Preference Intensity Value ( $I$ ) is a real value between  $-1$  and  $1$ . Negative preferences are expressed using any value in  $[-1, 0)$ ;  $-1$  is used to express complete dislike. Positive preferences are expressed using any value in  $(0, 1]$ ;  $1$  is used to capture the most likability. Equality/indifference is expressed using  $0$ .

**Diversity.** We measure the diversity of a set of items  $S$  by measuring how dissimilar, i.e., the semantic distance beyond a threshold, each item in  $S$  is with respect to all other.

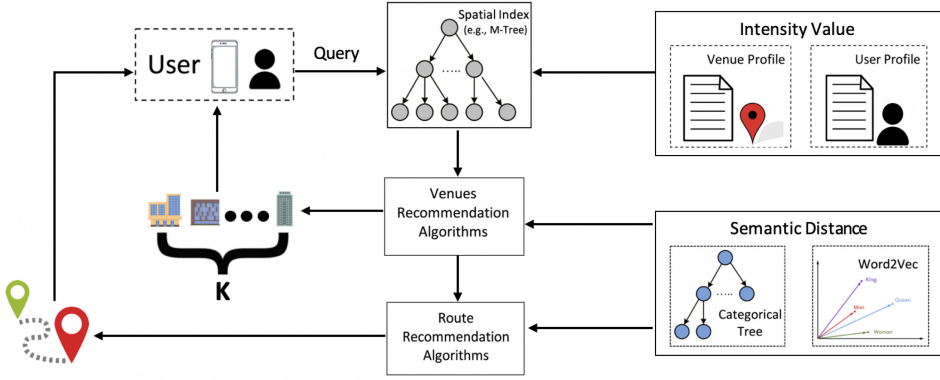


Fig. 2. MPG system architecture.

**Definition 4.** Dissimilarity: Let  $O$  be the set of items in the database. Two objects  $o_i$  and  $o_j \in O$  are dissimilar to each other  $dsm_\varrho(o_i, o_j)$  if  $dt(o_i, o_j) > \varrho$  for some distance function  $dt$  and a real number  $\varrho$ , where  $\varrho$  is a distance parameter, which we call radius.

**Definition 5.** Similarity: Two objects  $o_i$  and  $o_j \in O$  are similar to each other if  $dt(o_i, o_j) \leq \varrho$  for some distance function  $dt$  and a real number  $\varrho$ . We use  $sim_\varrho(o_i, O)$  to denote a set of items in  $O$  that are similar to an item  $o_i$ , such that  $\forall o_j \in sim_\varrho(o_i, O), o_j \neq o_i$ .

**Definition 6.** Coverage: Given a set of items  $S$  and a result-set  $R$ , where  $R \subseteq S$ , coverage corresponds to the percentage of items in  $S$  that satisfies  $dt(o_S, o_R) \leq \varrho$ , such that  $o_R \in R$  and  $o_S \in S$ , where  $dt$  is some distance function and  $\varrho$  is a real number parameter.

### 3.2 MPG Objective—Problem Statement

We first formulate the algorithmic problem that lays in the epicenter of MPG and then discuss the components of our solution.

**PROBLEM 1.** Given a set of geographical points  $G = \{g_1, g_2, \dots, g_l\}$ , a popularity index  $\xi_{g_i}$  for location  $g_i$ , a query point  $q$ , a reach  $r$ , a desired level of serendipity  $\psi$ , and a profile set that encodes user preferences  $\mathcal{P} = \{p_1, p_2, \dots, p_n\}$  and identifies a set  $G^* \subseteq G (|G^*| = k)$  with maximized diversity  $\Delta(S)$ , while satisfying the constraint set  $h(G^*, \mathcal{P}, q, r, \psi, \xi)$ .

In our setting, the set  $G$  corresponds to the set of available venues/PoI. The query point  $q$  corresponds to the current location of the mobile user, while  $r$  represents the maximum allowed distance between  $q$  and any point in the chosen solution  $V^*$ , and  $\psi$  indicates whether serendipity would be involved in the query. The set of preferences  $\mathcal{P}$  captures the profile of the mobile user with respect to his/her interests. Finally, the constraints described by function  $h$  include: (i) a geographic constraint that ensures that the maximum distance between the currently location of the mobile user and any venue recommended does not exceed  $r$  (i.e.,  $d(q, v_i) \leq r, \forall v_i \in V$ ); and (ii) a personalization constraint that ensures that the output set of venues is compatible with the user preferences (i.e.,  $V \models \mathcal{P}$ ).

Given this problem setting, the actual MPG system includes an interface that will obtain the following: (i) the current location of the user  $q$  (e.g., through the GPS sensors, NFC sensors); (ii) the user inputs such as the reach  $r$ ; and (iii) the set of types of venues she is interested in and the number of venues  $k$  she would like to know about. The preference of the user will be stored either in the system (i.e., bound to the user account) or stored on the mobile device and uploaded to

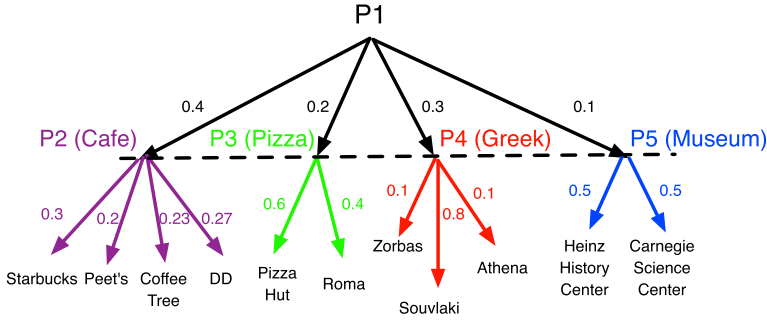


Fig. 3. Pam’s sample hierarchical user profile. The first level corresponds to the coarse-grained preference profile ( $P_1$ ), while each one of the sub-trees stemming from  $P_1$  corresponds to the preferences within each category (e.g., preference  $P_2$  corresponds to the “Cafe” venue type).

the system/server at the time of the request. In response to a request, MPG provides a set  $V^*$  of the recommended venues based on the definition of Problem 1. These recommended venues can further be used for route recommendations if desired or requested.

### 3.3 Venue Preferences

MPG utilizes a hierarchical profile  $\mathcal{P}$  that mirrors the typical venue classification. In the typical classification every venue  $v$  is associated with a categorical type  $\mathcal{T}_v$ , and every category may be a subcategory of another category. For example, an Italian pizzeria belongs to the category “Italian restaurant,” which can belong to the higher-level category “Restaurants,” which can itself belong to the category “Food,” and so on. At the top level of the hierarchy there are 10 categories, namely, *Arts & Entertainment*, *College & University*, *Food*, *Nightlife Spots*, *Outdoors & Recreation*, *Events*, *Professional & Other Places*, *Residences*, *Shops & Services*, and *Travel & Transport*. However, to build highly personalized and specific profiles, we use the bottom layer of hierarchy, as well as the specific venues visited.

In particular, given the set of check-ins  $C_u$  of mobile user  $u$ , we build a hierarchical profile  $\mathcal{P}$ . At the top level, the preferences of the user are expressed in terms of the (normalized) frequencies of this user’s visitations with respect to the types of venues. The second layer of the user profiles further provides the normalized frequencies of venues for the different types of locations visited by  $u$ . Figure 3 presents a sample profile for user Pam in our example scenario (in Section 1). Preference  $P_1$  is a coarse-grained preference profile, which informs the system that Pam prefers to spend 40% of her time in coffee shops, 10% in museums, 20% in burger joints, and 30% in Greek restaurants. Preferences  $P_2 - P_5$  are able to distill further Pam’s preferences. For instance, she appears to prefer Starbucks more than Peet’s coffee. Such a preference profile can nowadays easily be constructed with a variety of services, e.g., Google Maps Timeline; a detailed discussion around the construction remains outside the scope of this article. In our prototype implementation, we combine the user check-in information from Foursquare with the foursquare category hierarchy to build the user profiles [1].

### 3.4 MPG Intensity Value

MPG utilizes a preference intensity value for relevance that is a composite of syntactic-based and semantic-based intensity values: *distance-based*, *popularity-based*, and *profile-based* intensity values.

**3.4.1 Distance-based Intensity Value.** The physical distance between the current location  $q$  of the mobile user and venue  $v$  can also be used to obtain an intensity value for  $v$ . In particular with  $d_q^v$  being the normalized distance between  $q$  and  $v$ 's location the distance-based intensity value can be defined as:

$$I_d^v = 1 - \frac{d_q^v}{r}. \quad (1)$$

In the above equation, the distance has been normalized based on the maximum allowed distance from Problem 1, that is,  $r$ . Note here that  $d_q^v$  can be, in principle, equal to 0. However, this happens when the current user location  $q$  is at a venue  $v$ . Given that the user is already at this location, these venues are not considered by our system.

**3.4.2 Popularity-based Intensity Value.** An important factor that can impact the choice of a venue  $v$  from MPG is its popularity. With  $c_v$  being the number of total visits in venue  $v$ , i.e., the number of check-ins in  $v$ , and  $s_v$  being the number of unique visitors in  $v$ , we define the popularity-based intensity value of  $v$  as:

$$I_p^v = \lambda \cdot \frac{c_v}{\max_{i \in V} c_i} + (1 - \lambda) \cdot \frac{s_v}{\max_{i \in V} s_i}, \lambda \in [0, 1], \quad (2)$$

where  $V$  is the set of all the venues and  $\lambda$  is a scaling factor between the total number of visitors and the number of unique visitors. When  $\lambda = 1$ , only the number of total visitors determine the popularity-based Intensity value of a venue and when  $\lambda = 0$ , only the number of unique visitors determine the popularity-based Intensity value of a venue. The default is  $\lambda = 0.5$ . This intensity value essentially corresponds to the popularity index  $\xi$  used in the formal definition of the MPG problem.

**3.4.3 Profile-based Intensity Value.** The degree or strength of relevance of a venue  $v$  is expressed by the preference-based intensity value  $I_u^v$  derived from the user's profile. In particular, the profile-based intensity value is a combination of the score of the type of the venue (i.e., the coarse-grained preference) with the specific venue (i.e., fine-grained preference) score. As stated above, since these scores are derived from the user's check-ins  $C_u$ , the profile-based intensity value  $I_u^v$  for venue  $v$  and user  $u$  is computed as follows:

$$I_u^v = \omega \cdot \frac{C_u^v}{\sum_{v_j \in t} C_u^{v_j}} + \omega \cdot \frac{\sum_{v_j \in t} C_u^{v_j}}{\sum_{t \in T} \sum_{v_j \in t} C_u^{v_j}}, \quad (3)$$

where  $\omega$  is the tradeoff parameter between the coarse-grained and fine-grained preference scores with a default of 0.5,  $C_u^v$  is the number of check-ins that  $u$  had in  $v$ ,  $t$  is the venue type of  $v$  and  $T$  is the set of all venue types. Going back to Pam's case (Figure 3), the coarse-grained preference score would reflect her preference toward the nodes in the second level of her hierarchical user profile (i.e., Cafe, Pizza, Greek, and Museum), and the fine-grained preference score would be her preference toward the leaf nodes of her hierarchical user profile.

**3.4.4 Composite Intensity Value.** Having distance-based intensity value  $I_d^v$  and popularity-based intensity value  $I_p^v$ , we can combine them in one intensity score as follows, with  $\gamma$  the scaling factor:

$$I_{d,p}^v = \gamma \cdot I_d^v + (1 - \gamma) \cdot I_p^v, \gamma \in [0, 1]. \quad (4)$$

We can further combine  $I_{d,p}^v$  with profile-based  $I_u^v$  in a manner similar to Equation (4) and obtain a value that combines the profile preference, the popularity, and the distance of the venue from

the current location of the user. More specifically:

$$I_{u,p,d}^v = \alpha \cdot I_u^v + (1 - \alpha) \cdot I_{d,p}^v, \alpha \in [0, 1]. \quad (5)$$

Equation (5) combines three different elements (user preference through  $I_u^v$ , venue popularity through  $I_p^v$  or  $I_{p,\pi}^v$  and geography through  $I_d^v$ ) into a single intensity score. This combined score is the composite MPG intensity value of  $v$ ,  $I_k^v$ . Here, we would like to emphasize that the order with which we combine the three intensity values (i.e.,  $I_u^v$ ,  $I_p^v$  (or  $I_{p,\pi}^v$ ), and  $I_d^v$ ) to obtain  $I_k^v$  (or  $I_{k,\pi}^v$ ) does not impact the recommendations of MPG. This is due to the fact that MPG outputs a total order of the venues based on these three factors. The absolute values themselves for  $I_k^v$  will be different, but the order will always be the same. Furthermore, to provide an additional degree of personalization, each of the above functions includes adjustable tradeoff parameters (i.e.,  $\alpha$ ,  $\gamma$ ,  $\lambda$ ,  $\omega$ ) that are personalizable with respect to user interest.

Based on the above discussion, the results of the composite intensity value (i.e., Equation (5)) can be obtained in constant time  $O(1)$ . Therefore, the overall runtime per query for computing composite intensity value for each user query is linear with respect to the number of the initial set candidate venues involved in the user's range query.

### 3.5 The Semantic Similarity Measurement

In order for MPG to produce semantically diverse results, there must be a way to measure the semantic distance between two venues. Due to the ambiguous nature of venues, it is challenging to obtain a precise measure between an arbitrary pair of venues. To address this challenge, we propose a two-part semantic similarity measure that combines both the categorical information of the venue and the semantic of the venue's name to produce the accuracy measure of semantic similarity between any pair of venues. Next, we discuss the details of our semantic distance function.

**3.5.1 Category Tree.** As mentioned previously, MPG leverages the Foursquare Category Hierarchy [1] to derive the user preferences and build user profiles. However, such information can also be used to determine the similarity among venues. In particular, MPG accelerates both operations by constructing a *category tree* to capture the category structure of venues in Foursquare as a tree. Each internal node in the category tree represents a type of venue, where each internal node represents the subcategory of the parent node with each leaf node representing the actual venue. There are in total of 10 categories at the top level of this hierarchy. Each internal node in a category tree contains the following attributes: ID of the category it represents, the name of the category, a pointer to the parent node, and a list of pointers to each of its children nodes. Since a category tree can have an unlimited number of degrees, all of the children node pointers are stored as hash tables, with the key being venue ID and the value is the actual pointer.

The user profiles are further derived from the preference hierarchy, as described above in Section 3.3. The preference hierarchy consists of the top-level categories and the leaf nodes of the category tree (Figure 3). The category tree can be used to calculate the similarity distance between two venues  $v_i$  and  $v_j$  as follows:

$$Sim_{Tree}(v_i, v_j) = 1 - \frac{Ancestors\_Path}{Longest\_Path}, \quad (6)$$

where *Ancestors\_Path* is the number of common ancestors between the venues  $v_i$  and  $v_j$  and *Longest\_Path* is the number of nodes on the longest path to the root from either  $v_i$  and  $v_j$ .

**3.5.2 Name Semantics.** Although the category tree is able to measure the similarity between two venues, this measurement is not very accurate as it only provides a coarse granularity distance



between two venues. Specifically, this measurement cannot distinguish the difference between two venues that are under the same subcategory, for example, “McDonald’s” and “Burger King,” as both of them share the exact same ancestors.

Our hypothesis is that the names of venues reflect their identity/semantics in a finer granularity than their category type. Therefore, to overcome this limitation, MPG utilizes Word2Vec [45], an advanced NLP technique, which supports fine granularity distance calculation between two venues by going beyond syntactic comparisons. Word2Vec provides the implementation of two word-vector representation computing models: *Continuous Bag-of-Words* model (CBOW), which predicts the current word based on the sourcing words, and *Continuous Skip-gram* model, which seeks to use the current words to predict surrounding words. Both of these models are based on the Neural Net Language Model.

With Word2Vec, the similarity of word representations goes beyond simple syntactic regularities. Specifically, word vectors capture many linguistic regularities. For example, after obtaining the word representation in vector space, the resulting vector can have the following properties, such that  $\text{vector}(\text{'King'}) - \text{vector}(\text{'Man'}) + \text{vector}(\text{'Woman'})$  results in a vector that is closest to the vector(‘Queen’). MPG uses CBOW model to generate all word vectors.

The difference between two words under Word2Vec are calculated through the cosine similarity of two-word vectors, such that cosine similarity is defined as follows:

$$\text{Sim}_{Vec}(A, B) = \frac{\sum_{i=1}^n A_i B_i}{\sqrt{\sum_{i=1}^n A_i^2} \sqrt{\sum_{i=1}^n B_i^2}}, \quad (7)$$

where  $n$  is the length of vector,  $A_i$  and  $B_i$  are elements of vector  $A$  and  $B$ , respectively.

The current word vectors we adopted support phrases that consist of up to two words. For venue names that have more than two words or are not contained in the word vectors, we split the phrases into single words and then obtain word vectors for each individual word in the phrases. The final vector of a phrase is obtained through the average of all vectors for each word in this phrase. Since the accuracy of Word2Vec strongly depends on the quality of the word vectors, a large real-world corpus is needed to obtain high-quality word vectors. We have experimented with various corpuses in an attempt to generate the highest-quality word vectors. The best suitable word vectors we obtained were generated from the entire English Wikipedia that consists of 55 GB of plain text. The resulting word vectors contain over 4 million entries. To effectively query the word vectors, MPG stores all the word vectors in memory as a hash map.

Similarly to category-tree-based similarity, the Word2Vec-based similarity has its own biases. We were able to overcome these biases of the individual similarity metrics by combining them (Equations (6) and (7)) and measuring the similarity between two venues  $v_i$  and  $v_j$  as follows:

$$\text{Sim}(v_i, v_j) = \frac{\text{Sim}_{Tree}(v_i, v_j) + \text{Sim}_{Vec}(A, B)}{2}, \quad (8)$$

where  $A$  and  $B$  are representing the vector representation of venue  $v_i$  and  $v_j$ , respectively.

Note that for efficiency purposes, both Category Tree and Word2Vec have been cached in main memory as hash tables. This allows MPG to compute the above composited semantic distance (i.e., Equation (8)) in constant time for each venue and, in turn, enable a linear runtime complexity for each user query.

### 3.6 Spatial Indexing Structure

One of the main operations in MPG is to generate a set of nearby neighbors. To speed up this process, MPG utilizes the widely adopted *M-tree* spatial index structure [13]. *M-tree* uses triangle inequality for efficient range queries, similarly to those required in MPG. An *M-tree* is a balanced tree index that

is designed to handle a large scope of multi-dimensional dynamic data in general metric spaces. An M-tree partitions the space in such a way that it generates spherical boundary regions around some of the indexed items, called *pivots*, with some bounding radius  $r$ . Each internal node has at most  $N$  entries and contains the following attributes: a pivot  $p_v$ , the bounding radius  $r$  around  $p_v$ , a pointer  $pt$  to the subtree that is rooted in the pivot  $p_v$ , and the distance between  $p_v$  and its parent pivot. The distance of a subtree from  $p_v$  is guaranteed to be within the bounding radius  $r$ . Each leaf node in the tree has two attributes: the item that is being indexed and the distance between this leaf node and the parent pivot. The efficiency of M-tree has been proven in a large body of existing works (e.g., Reference [19]), and a detailed cost model for M-Tree's search complexity can be found in Reference [14].

#### 4 MPG'S SERENDIPITY ALGORITHMS

In this section, we introduce the key algorithmic components of MPG, particularly the venue and route recommendation algorithms, which produce relevant, diverse, and yet unpredictable results within a specified latency requirement.

##### 4.1 Venue Recommendation Algorithm

As discussed earlier in Section 1, serendipity is an important concept in helping recommendation algorithms improve user satisfaction, which is focused on recommending items that are relevant while unexpected. To achieve the conflicting objectives of serendipity in recommend *relevant* while *unexpected* venues, we incorporated the serendipity under the algorithmic framework of our previously proposed algorithm *Preferential Diversity* (PrefDiv) [23] that produces a set of recommendations, which balances the tradeoff between relevance and diversity in an efficient manner. In fact, PrefDiv provides parameter  $A$  to tune the balance between relevance and diversity in the returned result set of recommendations  $R$ . When  $A = 1$ ,  $R$  would simply be the top- $k$  items from the initial set, i.e., the items with the  $k$  highest intensity values, and when  $A = 0$ ,  $R$  contains  $k$  dissimilar items from the initial set. Since PrefDiv is an iterative algorithm, in the case  $A$  is in between 0 and 1, the final results will contain at least  $A * k$  items from every iteration, and in each iteration,  $A$  will be divided by half.

The basic logic of PrefDiv (Algorithm 1) is as follows: It first sorts the objects in the initial set  $O = \{o_1, \dots, o_n\}$  in descending order of their intensity values and splits them into groups of  $k$  objects. In each iteration, it evaluates the objects in a group for diversity, starting with the group that contains the highest intensity objects (Lines 4 and 5). Item  $o_i$  with the highest  $I_u^{o_i}$  in the group  $T_O$  is moved into the final result set  $R$ , if there is no object in  $R$  similar to  $o_i$ , i.e.,  $\text{sim}_Q(o_i, R)$  is empty; otherwise, it is marked as "Eliminated." Also, all objects in  $\text{sim}_Q(o_i, T_O)$  are marked as "Eliminated." While there are still objects left in  $T_O$  that are not being marked as "Eliminated," it processes the next unmarked one  $o_j$  with the highest  $I_u^{o_j}$  in the same manner (Lines 6–13). Note that the *Accept()* function on Line 9 always returns True for PrefDiv, as it is designed for *pPrefDiv*, as discussed below. PrefDiv ends an iteration by finalizing the moving of objects into  $R$  according to  $A$ , as mentioned above. If fewer than the required  $A * k^{\text{iter}}$  objects were moved in  $R$ , then the difference  $s$  is covered by moving the top  $s$  objects with the highest intensity values that have been marked as "Eliminated" in  $T_O$  into  $R$  (Lines 14–16). The iterations continue until either  $k$  objects are selected ( $|R| = k$ ) or if all items in  $O$  are examined. If the size of  $R$  is still less than  $k$ ,  $k - |R|$ , then items with the highest intensity values that have been marked as "Eliminated" will be selected and added to  $R$  (Lines 17–22).

The adoption of PrefDiv helps to ensure the recommended results are relevant to the user's intent. However, PrefDiv is a deterministic algorithm, and, thus, it does not incorporate the concept of serendipity. To introduce serendipity in PrefDiv, we devise a non-deterministic version of

*PrefDiv*, coined *Probabilistic Preferential Diversity* (*pPrefDiv*). *pPrefDiv* offers serendipity through probability weighted by relevance. In contrast to *PrefDiv*, when a venue  $x$  is qualified to be one of the recommendations for a range query  $q$ ,  $x$  is not automatically included in the result set (Line 9:  $Accept(x) = True$ ). Instead, *pPrefDiv* decides whether or not  $x$  can be added to the result based on the following probability:

$$p(x \text{ is accepted}) = \frac{CI(x)}{\text{Argmax}_{i \in O} CI(i)}, \quad (9)$$

where  $CI(x)$  is the composited intensity value of  $I_d^v$ ,  $I_p^v$ , and  $I_u^v$  of a venue  $x$  and  $O$  is the set of all venues within  $q$ . In the case of *pPrefDiv*, this probability (i.e., Equation (9)) is computed for each  $x$  by the  $Accept()$  function on Line 9 of Algorithm 1. If  $x$  is accepted (Line 9), then it will be presented as one of the recommendations. Otherwise,  $x$  will be discarded, and *pPrefDiv* would proceed to the next venue.

For example, assume  $O = \{o_1, \dots, o_n\}$  is the initial set of venues,  $R$  is the set of result that *pPrefDiv* is producing,  $o_u$  is an unmarked venue that has a composited intensity value of 0.6, which is currently the highest among all unmarked venue in  $O$ , and there is no object in  $R$  similar to  $o_i$  (i.e.,  $sim_q(o_i, R)$  is empty). According to *PrefDiv*,  $o_u$  should be included in the result-set. However, *pPrefDiv* would use intensity value weighted probability to determine the acceptance of  $o_u$ . For instance, if the highest composited intensity value in  $O$  to be 0.8, then  $o_u$  would have a probability of  $0.6/0.8 = 75\%$  to be included in the result-set.

The introduction of randomness by means of a composited intensity value-based probability allows *pPrefDiv* to incorporate serendipity into the venue recommendations, while still preserving the high-intensity value and semantic distance feature of the *PrefDiv* algorithms.

**Time Complexity.** According to the above discussion (Algorithm 1), we can observe that the worst case complexity of *pPrefDiv* is  $O(kN)$ . Fortunately, as the size of  $k$  is usually a small number, *pPrefDiv* should typically behave as a linear algorithm. Furthermore, as we will show in our empirical studies (Section 6), depending on the diversity constraints, *pPrefDiv* typically does not need to examine all original items. That is, a very small set of items would be sufficient enough to produce  $R$  if the radius is appropriately defined.

## 4.2 Route Recommendation Algorithm

By employing *pPrefDiv*, MPG is capable of producing informative recommendations, which significantly benefits the user's exploration of cities. However, the best route that the user can take to visit these recommended venues remains to be decided. Thus, MPG further supports route recommendations that are constructed based on the recommended venues with variable length.

To incorporate serendipity in the recommendation of routes, for a user-defined route length  $k$ , where  $k$  is the number of venues that comprise a route, we utilize random walks to generate sets of initial routes.

**Random Walks.** The random walks are performed on a weighted graph between the venues. The weight  $w_e$  of edge  $e$  considers the distance between the current location of the user, the number of visits to the venue, and the user's preference toward a certain type of venue. The probability that our random walk will go through edge  $e$  is proportional to  $1/w_e^\gamma$ , where  $\gamma$  is a system parameter. The weight assigned is a tunable parameter that users can explore. Before generating the final route recommendations, we perform a number of  $\xi$  random walks to yield the initial set of candidate routes. Such serendipity incorporated by the random walks is essential to enable the MPG to yield unexpected, yet interesting route recommendations to the user. Since the complexity for generating one random-walk path is simply  $O(k)$ , the total time complexity for random-walks-based routing is simply  $O(\xi k)$  per each user query.

**ALGORITHM 1:** PrefDiv/pPrefDiv Main**Require:**

1: Set of objects  $O$ , a size  $k$ , a radius  $\rho$  and  $A$  tuning parameter

**Ensure:**

```

2: One subset  $R$  of  $O$ 
3:  $S \leftarrow \emptyset$ 
4: while there exists unmarked items in  $O$  and  $|R| < k$  do
5:    $S \leftarrow$  Pick  $k$  items with highest composited intensity from  $O$ 
6:   for all  $o_i \in R$  do
7:     mark  $\forall o_j \in \text{sim}_\rho(o_i, S)$  as "Eliminated"
8:   for all unmarked items  $o_i$  in  $S$  do
9:     if  $\text{Accept}(o_i)$  then
10:        $R = R \cup o_i$ , s.t.  $o_i \in S$  is unmarked and  $I_u^{o_i} \geq I_u^{o_j} : \forall o_j \in S$ 
11:       for all unmarked  $o_u \in S$  do
12:         if  $o_u \in \text{sim}_\rho(o_i, S)$  then
13:           mark  $o_u$  as "Eliminated"
14:       while number of unmarked items in  $S < A \cdot k$  do
15:          $R = R \cup o_i$ , s.t.  $o_i \in S$  is unmarked and  $I_u^{o_i} \geq I_u^{o_j} : \forall o_j \in S$ 
16:        $A = A \cdot 0.5$ 
17:       if first iteration then
18:         create new set  $G \leftarrow \forall o_j \in S$ , s.t.  $o_j$  is marked
19:        $O = O - (O \cap S)$ 
20:   if  $|R| < k$  and  $\forall o_j \in O$ , s.t.  $o_j$  are marked then
21:     while  $|R| < k$  do
22:        $R = R \cup o_j$ , s.t.  $o_j \in G$  and  $I_u^{o_j} \geq I_u^{o_i} : \forall o_i \in G$ 
23: Return  $R$ 

```

Using this initial set of  $\xi$  routes, we determine our final recommendations by introducing the quantitative measurements of serendipity. Since serendipity implies that the recommended routes should be unexpected by the user, therefore, to capture this unexpectedness, we first have to determine the most intended (i.e., expected) route, and then measure the difference between the recommended route and the most intended route. As we have modeled the user's intention using the intensity score, thus, the routes  $r_I^*$  constructed based on the ranking of the intensity value naturally represents the most intended route.

**HighestRelevance.** We propose *HighestRelevance* as the method to construct routes based on the ranking of intensity value. For a given set of object  $O$ , such that  $|O| = k$ , and a length  $k'$ , where  $k' < k$ , *HighestRelevance* constructs a route of length  $k'$  by selecting the first  $k'$  objects with highest composited intensity value from  $O$  and then ordering each object in descending order according to their combined intensity value. Whenever possible, *HighestRelevance* always seeks to separate two venues with the same category (according to the category tree) and thus to improve the usability of the route by preventing two venues with the same category to be visited in sequence.

**Serendipity Metric.** To measure the serendipity of a given route  $r$ , we first find the set of overlapping venues  $O_{r, r_I^*}$  between  $r$  and the route that maximized the intensity value  $r_I^*$ . Based on the set of overlap venues we compute the *Overlap Factor* (*OvF*) between  $r$  and  $r_I^*$  as follows:

$$\text{OvF}(r, r_I^*) = 1 - \frac{|O_{r, r_I^*}|}{|r|}. \quad (10)$$

Then we compute the *Normalized Longest Common Subsequence* (NLCS) between  $r$  and the route that maximized the overall intensity value  $r_I^*$  as follows:

$$NLCS(r, r_I^*) = \frac{|L_{r, r_I^*}|}{|r|}. \quad (11)$$

Thus, the serendipity  $\sigma_r$  of  $r$  would be

$$\sigma_r = (1 - NLCS(r, r_I^*)) * OvF(r, r_I^*). \quad (12)$$

The idea for quantifying the serendipity of a route by measuring its normalized longest common subsequence and overlap factor with the route  $r_I^*$  that has the maximum overall intensity value is because  $r_I^*$  is the most anticipated route based on prior knowledge. Therefore, routes with large deviation from the most anticipated route can be considered as less expected and thus have higher serendipity.

**Pareto Front.** The quality of the recommended venues with respect to the relevance is ensured by the venue recommendation algorithm employed. However, as the length of the routes could be much shorter than the number of recommended venues, diversity becomes an issue as routes that consist of only venues that are semantically close to each other (e.g., belongs to the same category). Such routes are typically considered as not interesting routes. To prevent this issue, rather than optimizing over a single dimension, MPG computes the Pareto Front of the random walks generated based on their serendipity  $\sigma_r$ , as described above (Equation (12)), and their diversity  $\delta_r$  [24]. The Pareto Front includes the non-dominated points, which is a set of points that can no longer be improved along one dimension without sacrificing the others, i.e., a route  $r$  is part of the Front *iff*  $\sigma_r \geq \sigma_{r'}$  and  $\delta_r \leq \delta_{r'}$ ,  $\forall r' \in \mathcal{R}$ , where  $\mathcal{R}$  is the set of the random walks.

Given the fact that the computed Pareto Front might include a large number of routes, we divide it into  $n$  equal parts (through projections on the dimension with the maximum range), where  $n$  can be adjusted by the user, and choose a representative route for each part of the front based on the shortest distance to be covered. This ensures our system will provide the user with multiple alternative routes that capture different levels of the tradeoff between both serendipity and diversity dimensions.

## 5 PROTOTYPE IMPLEMENTATION

We have implemented a prototype MPG both as a web service and a mobile app for Android devices. We further developed a testbed, namely, Experimental Platform for Urban Informatics (EPUI)<sup>2</sup> [26], to evaluate the effectiveness of our proposed mobile service MPG and explore our ideas for capturing serendipity.

EPUI consists of a user-friendly front-end interface and an efficient back-end server that incorporates our proposed venues recommendation algorithms as well as other components of MPG. Further, EPUI supports a number of different approaches for the venue and tour recommendations based on the user's current location, which enables the user to compare the recommendations of different recommendation engines by both presenting the recommended venues and tours visually on the map as well as displaying evaluation metrics through summary dashboards.

Specifically, EPUI implements the following well-known venue recommendation algorithms: DisC Diversity [19], K-Medoid, and the Random Selection-based recommendation approach. In addition to these algorithms, EPUI enables the user to compare the performance of different venue recommendations and route construction approaches, including our proposed MPG service, as well as the user's own customized algorithm to facilitate the research and development in both venue

<sup>2</sup> An introduction video can be found at <http://tiny.cc/sf0d7y>.



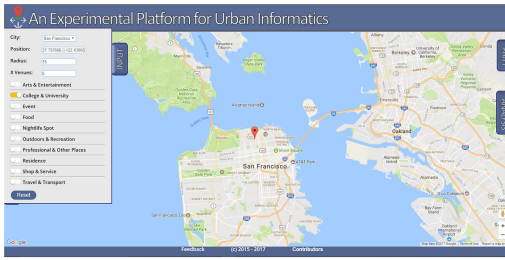


Fig. 4. EPUI Input Panel.

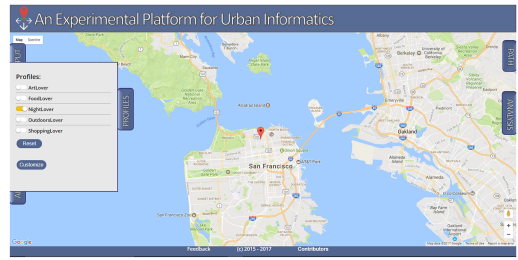


Fig. 5. EPUI Profile Panel.

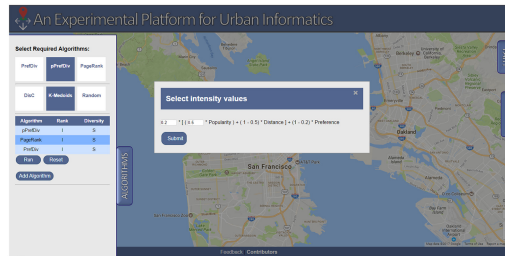


Fig. 6. EPUI Algorithms Panel.

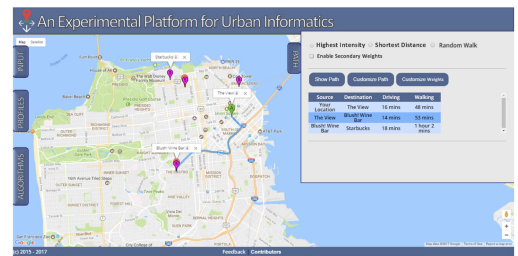


Fig. 7. EPUI Display Results.

recommendation and route construction. For example, while we have implemented the same diversity scheme for all algorithms, our implementation is flexible and allows for different diversity and indexing schemes that can easily be adjusted by the user.

The front-end of EPUI is constructed from javascript and PHP with the help of Google Maps API for visualizing the results on a map. It communicates with the back-end server through JSON and currently supports the cities of New York, San Francisco, and Pittsburgh. The recommended venues or POIs are numbered and colored to match the number and the color of the algorithm making the recommendation, along with different provisions to drive or walk to those recommendations. The interface consists of five different panels: “Input,” “Profile,” “Algorithms,” “Path,” and “Analysis” (Figures 4–6).

The “Input” panel provides the options for the user to specify the inputs that describe the basic information for each query, such as the radial distance they are willing to travel, the number of venues they would like to get returned, and the types of venues they are interested in exploring (Figure 4).

The “Profile” panel provides the options for the user to specify their own preferences by selecting any of the predefined profiles (i.e., *ArtLover*, *FoodLover*, *OutdoorsLover*, etc.) (Figure 5) or to customize a selected preference profile by adjusting the values on the corresponding entry of the category tree.

The “Algorithms” panel (Figure 6) allows users to choose, customize, and upload the recommendation algorithm(s) that would be involved in the location query. To upload an algorithm, EPUI simply requires the user to providing the name and the corresponding template java program, and then it will be include in the algorithms list along with other existing algorithms. For each algorithm, the user has an option for adjusting the composition of the ranking (Equation (5)) and semantic distance (Equation (8)) function.

The “Analysis” panel visualizes the performance characteristics of the recommended venues from the selected algorithms in tabular form as well as in a scatterplot. The listed characteristics

in terms of quality are the relevance score of the recommended venues, their diversity, and the radius of gyration for each set of the recommended venues. We also report the runtime taken for each algorithm as an indicator of interactivity.

The “Path” panel (Figure 7) allows users to select the construction method of the routes based on sets of recommended venues and a route network graph  $G$ . Once a route construction method has been selected, it would determine the visit sequence of each recommended venues. Later, the route that connects each venue (according to the specified sequence) would be constructed based on the weights assigned on  $G$ . Furthermore, users are able to assign any weights to the edges of  $G$  by upload their customized weight modules as well as specify their desired tradeoff between weights that are currently assigned to each edge of  $G$ . Finally, this panel also includes a statistics table that would display basic informations (e.g., originate, destination) or evaluation measures (e.g., distance, risk, relevance, diversity) according to the user’s configuration.

## 6 PERFORMANCE EVALUATION

In this section, we present the detail evaluation of our proposed mobile service MPG using our experimental platform EPUI and real-life data. Before discussing our findings, we introduce the datasets used in our experimental evaluation.

### 6.1 Datasets

In our experiments, we used data collected across five months from Foursquare. Foursquare is a major digital, location-based social network where the main interaction among its users is the voluntary sharing of one’s whereabouts through *check-ins*. Foursquare has a rich, user-curated venue database through which users can choose to notify their friends of their current location. Furthermore, as mentioned in Section 12, we have used a Word2vec model that is trained on the entire English Wikipedia. Note that this is the only MPG component that requires training data for model training, and since it is used as a semantic distance measure, we did not create a separate English Wikipedia testing data to test the performance of the word vector obtained from Word2vec. In particular, our study utilizes the following information:

**Venue database:** We used Foursquare’s public venue API and queried information for **14,011,045** venues. Each reading has the following tuple format:  $\langle \text{ID, latitude, longitude, \# check-ins, \# unique users, type} \rangle$ . The purpose of this dataset is twofold: (i) obtain a database of all points-of-interest (POIs) in a city and (ii) to obtain information that can be used as a proxy for the quality of a venue (e.g., the number of unique users that have checked-in to the venue or the total number of check-ins). We have queried the Foursquare venue database and have obtained the relevant information for all the venues in New York City (NYC), San Francisco (SF), and Pittsburgh (PIT) (depicted in Figure 8).

Figure 8 shows the population for the three respective cities when splitting into nine equal-width partitions. The total number of venues for each city is (i) 471,052 in NYC, (ii) 73,623 in SF, and (iii) 33,975 in PIT, and the standard deviation among the buckets for each city is (i) 80K in NYC, (ii) 8.6K in SF, and (iii) 5.5K in PIT.

**User check-in information:** User preferences can be indirectly revealed through their historic visitations (e.g., frequent visits at Chinese restaurants by Pam is a strong signal for her appeal to this cuisine). To build realistic user profiles for our evaluations, we used a dataset collected by Cheng et al. [12] that includes geo-tagged, user-generated content from a variety of social media between September 2010 and January 2011. This dataset includes 11,726,632 Foursquare check-ins generated by 188,450 users.

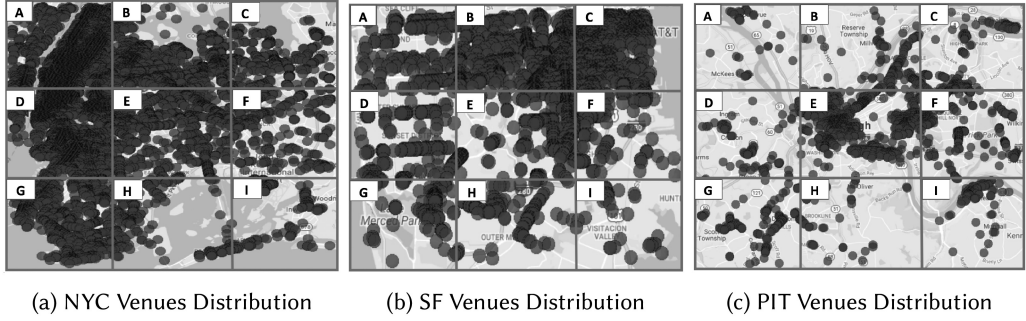


Fig. 8. Spatial visualization of datasets population for an indicative 3x3 partitioning.

Table 1. Model Abbreviation

Models	Description
PD(composite)	Uses composite intensity value as the relevance score for <i>PrefDiv</i> .
pPD(composite)	Uses preference-based intensity value as the relevance score for <i>pPrefDiv</i> .
DisC	Only uses the result of DisC Diversity [19] as the final ranking without using <i>PrefDiv</i> .
<i>k</i> -Medoids	Only uses the result of <i>k</i> -Medoids as the final ranking without using <i>PrefDiv</i> .
Random	Only uses the randomly selected result as the final ranking without using <i>PrefDiv</i> .

## 6.2 Evaluation of POIs Recommendation

In this section, we will provide a detailed comparison between our proposed *pPrefDiv* with a number of baseline algorithms (as listed in Table 1) for POIs recommendations.

**6.2.1 Methodology.** In our evaluation, we have employed as baselines a number of algorithms, including DisC Diversity, which is the state-of-the-art diversification algorithm that optimizes the coverage of the result-set. We also included one well-known clustering algorithm, *k*-Medoids [49], which aims to group a set of data objects into clusters through some distance measure, so each object within a cluster are close to each other and objects outside of the cluster are disclosed to the objects inside the cluster. In our experiment, we have implemented *k*-Medoids based on Reference [49]. Since *k*-Medoids does not capture the relevance in any regard, we thus improved the performance of *k*-Medoids in balancing the relevance-versus-diversity tradeoff by choosing the object with the highest intensity value as the final recommendation from each of its *k* clusters. This improvement significantly enhances the performance of the *k*-Medoids with respect to relevance while exhibiting the minimum decrease in diversity. In addition, we also employed the random selection of venues as another baseline to show the effectiveness of our proposed methods.

For all algorithms involved in our experiments, we utilized the semantic distance measure (Equation (8)) as the way to measure the distance between two given points. Table 1 summarizes all models employed in our experiments, and the values of the parameters used are summarized in Table 2.

We ran all our experiments on a computer with Intel Core i7 2.5-GHz CPUs, 16-GB Memory, and 512-GB SSD and used the Foursquare datasets described in Section 6.1. We created individual Foursquare user profiles as described above and three super-user profiles with more fine-grained preferences by merging the profiles: (i) 1,000 Foursquare users (Super-user A); (ii) 500 Foursquare users (Super-user B); and (iii) 350 Foursquare users (Super-user C). Note that the Super-user A

Table 2. Parameter Configuration

Parameter	Value	Description
$\lambda$	0.5	scaling factor of number of visitors vs unique number of visitors
$\gamma$	0.7	scaling factor of distance-based intensity value vs popularity-based intensity value
$\alpha$	0.5	scaling factor between profile preference vs popularity vs distance of each
$\omega$	0.5	scaling factor of coarse-grain preference vs fine-grain preference
$\xi$	50	number of random walks to yield the initial set of candidate routes
$A$	0.3	relevance diversity trade-off parameter for PrefDiv
$\varrho$	0.7	threshold for define a pair of dissimilar venue
$K$	10–50	number of venues recommend in each query
Radius	1.5 km	the travel radius from user's current location
Number of Locations	15, 50	number of recommend venues
Number of Categories of POIs Selected	5, 10	number of POIs involved in the recommendation

contains both Super-user B and Super-user C, where Super-user B and Super-user C are two disjoint sets of profiles.

**6.2.2 Experimental Evaluation Metrics.** In our experimental evaluation, we use three well-known metrics: *Normalized Relevance* [54], *Average Similarity Distance* (based on semantic distance measure, Equation (8)), and *Coverage* [18].

**Definition 7 (Normalized Relevance).** Let  $O$  be a set of venues and  $O_k^* \subseteq O$  such that  $|O_k^*| = k$ . The Normalized Relevance of  $O_k^*$  is defined as the total relevance score of  $O_k^*$  over the sum of top- $k$  highest relevance scores of  $O$ .

In our experiments, Normalized Relevance is represented through two type of intensity values, *Normalized Composite Intensity Value* (NCI) and *Normalized Preference-based Intensity Value* (NPI).

We defined Normalized Composite Intensity Value as:

$$NCI(x) = \frac{CI(x)}{\text{Argmax}_{i \in O} CI(i)}, \quad (13)$$

where  $CI(x)$  is the composited intensity value (Equation (5)) of a venue  $x$  and  $O$  is the set of all venues within the currently range query  $q$ .

Normalized Preference-based Intensity Value is defined as:

$$NPI(x) = \frac{PI(x)}{\text{Argmax}_{i \in O} PI(i)}, \quad (14)$$

where  $PI(x)$  is the Preference-based intensity value (Equation (2)) of a venue  $x$  and  $O$  is the set of all venues within the currently range query  $q$ .

The reason to employ NCI and NPI as the relevance measure is to show how much the relevance has been preserved with respect to the given utility function. By comparing the aggregated intensity score of the recommended representative subset  $O_k^*$  with the  $k$  most relevant item (i.e., item with highest intensity according to the given utility function) of the original set  $O$ , one can clearly know the degree of the intensity value being preserved in the current representative subset  $O_k^*$ .

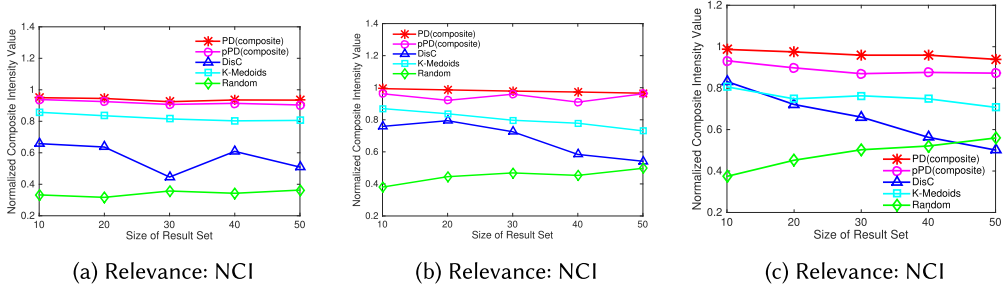


Fig. 9. Compare the relevance of different recommendation algorithms for NYC, SF, and PIT (Super-user A).

**Definition 8 (Average Similarity Distance).** Let  $O$  be a set of venues, the average similarity distance of  $O$  represents the average of the pairwise distances of the venues in  $O$ .

Due to the fact that two distinct instances in our dataset may be semantically duplicate venues (e.g., two difference Starbucks), our experiments normalize Average Similarity Distance (ASD) to take into consideration that different methods may return as a result of a list of venues with semantic duplicates rather than a set and expressed as Redundancy Normalized Pairwise Distance (RNPD):

$$RNPD(L) = \left(1 - \frac{|Unique(L)|}{|L|}\right) * ASD, \quad (15)$$

where  $Unique(O)$  represents  $O$  without duplicates.

The reason to employ RNPD as the diversity measure is to show how each item contained in a given representative set  $O_k^*$  is different compared to the rest of the items in  $O_k^*$ . The most intuitive way to do so is to measure the pairwise distance (with a given distance measure) between each pair of items, which is essentially the ASD defined above. Since recommending unique venues is important in the case of venue recommendation, we included a penalty (i.e.,  $(1 - \frac{|Unique(L)|}{|L|})$ ) for recommending two or more duplicate venues in the recommendation result set, which forms the Redundancy Normalized Pairwise Distance (RNPD).

**Definition 9 (Coverage).** Let  $O$  be a set of venues,  $O_k^* \subseteq O$  such that  $|O_k^*| = k$  and  $S \subseteq O$  be defined as the union of  $sim_{\varrho}(v_i, O)$  for all  $v_i \in O_k^*$ . The coverage of a subset  $O_k^*$  is defined as the percentage of venues in  $S$  over the total number of venues in  $O$ , i.e.,  $|S|/|O|$ .

As discussed with more detail in Reference [18], the reason to use coverage for evaluating the degree of coverage provided by a representative subset  $O_k^*$  is simply as it naturally represents the percentage of the item has been covered by  $O_k^*$  with respect to a given radius  $\varrho$ .

**6.2.3 Experimental Results.** In this section, we present the evaluation of all models in our experiments. Specifically, we will show a comprehensive set of comparisons between our proposed  $pPrefDiv$  and other alternative algorithms that show the capability of  $pPrefDiv$  in handling the POIs recommendation.

As we have demonstrated previously, PD(composite) has exhibited the best performance when compared to other PrefDiv-based models. We extend the same composition of the intensity value to the non-deterministic variance  $pPrefDiv$  (1), which is a variance of PrefDiv that incorporates the serendipity. Further, we compare PD(composite) (i.e., PrefDiv) and pPD(composite) (i.e.,  $pPrefDiv$ ) to other well-known algorithms to show the performance of both PrefDiv and  $pPrefDiv$ -based recommendation engine when compared to other existing alternatives.



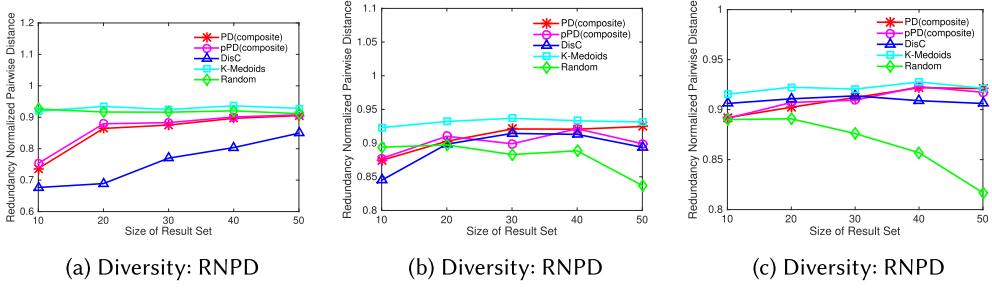


Fig. 10. Compare the diversity of different recommendation algorithms for NYC, SF, and PIT (Super-user A).

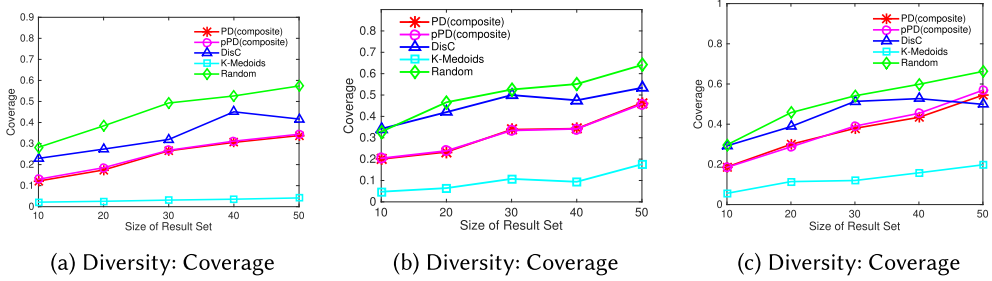


Fig. 11. Compare the coverage of different recommendation algorithms for NYC, SF, and PIT (Super-user A).

Figure 9(a), (b), and (c) shows the average normalized composite intensity value (NCI) of all models for New York City (NYC), San Francisco (SF), and Pittsburgh (PIT). In these results, both PrefDiv and pPrefDiv have constantly outperformed other alternatives in all three cities. In particular, PrefDiv and pPrefDiv have outperformed random by up to 263%, DisC by up to 93%, and  $k$ -Medoids by up to 36%. Among all involved algorithms,  $k$ -Medoids has performed second best after the PrefDiv and pPrefDiv, which is due to the reasons that we have implemented  $k$ -Medoids in a way that enhanced its ability to capture the relevance. Random achieves the worst performance, because the number of highly preferred venues is much less than the non-preferred venues; thus, blindly selecting venues would not deliver a good performance in terms of relevance.

Figure 10(a), (b), and (c) illustrates the Redundancy Normalized Pairwise Distance (RNPd) of all models for all three cities. Here we have seen that all algorithms have achieved overall better performance for RNPd when compared to NCI. This is as expected, since all involved algorithms except Random have been optimized toward the diversity. We noticed that Random also performs very well with respect to RNPd, which can be explained as follows. Since the number of neighbors of given venues (in terms of semantic distance) is always going to be much less than non-neighbors, those it is much easier for Random to generate a set of results that are semantically diverse than to generate a set of semantically similar results. Here, we have seen that although PrefDiv and pPrefDiv did not outperform all other alternatives, the price that both PrefDiv and pPrefDiv have paid to achieve the high relevance score (in terms of relevance and diversity tradeoff) is extremely small. When compared to the  $k$ -Medoids, which achieves the highest performance in semantic diversity, PrefDiv and pPrefDiv are still just slightly behind.

Figure 11(a), (b), and (c) demonstrates the performance of coverage of all models. In this set of results, we have seen that DisC and Random achieve the best performance in terms of coverage. This is as expected, as the DisC utilized a greedy-based approach that is specifically optimized

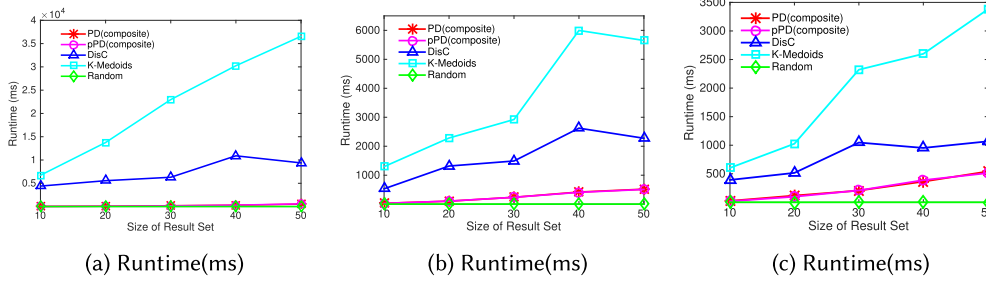


Fig. 12. Compare the runtime of different recommendation algorithms for different cities (Super-user A).

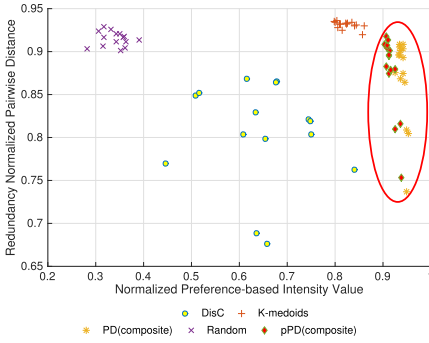


Fig. 13. Relevance vs. diversity (NYC).

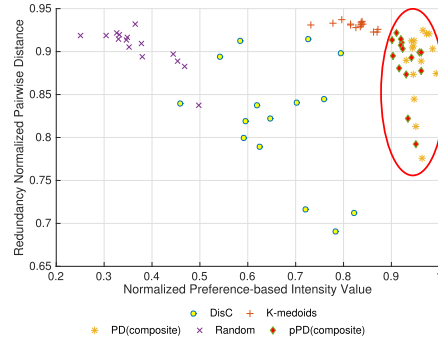


Fig. 14. Relevance vs. diversity (SF).

toward the coverage. As for the random, since it builds the result-set by evenly sample the venues across all candidate venues in a given spatial query, it thus has a high likelihood to achieve excellent coverage when dealing with datasets where data objects are distributed evenly across space. In the case of urban datasets, semantically closer venues are more or less distributed evenly across the city to prevent excessive competition and thus enable random to achieve high coverage. However, the difference between PrefDiv (as well as pPrefDiv) with random and DisC is not significant. Considering the performance advantage that PrefDiv and pPrefDiv have gained in the relevance, therefore both PrefDiv and pPrefDiv still served as a much better venue recommendation engine than other alternatives.

Figure 12(a), (b), and (c) demonstrates the runtime of all models for New York City, San Francisco, and Pittsburgh. Since the POIs recommendation involves humans in the loop, it is extremely important for the system to maintain an interactive response time. To achieve such a goal, it requires the algorithm to be as efficient as possible. From these experiments, we can see that both PrefDiv and pPrefDiv have outperformed DisC and *k*-Medoids in runtime by orders of magnitudes. The only alternative that is faster than our PrefDiv and pPrefDiv is the Random method; this is because it does not require any complex computations. Such a huge difference in efficiency has undoubtedly made the PrefDiv and pPrefDiv to be better choices for POIs recommendations.

Figures 13, 14, and 15 present three scatterplots from New York City, San Fransisco, and Pittsburgh, respectively, that showed the capability of each algorithm in balancing the tradeoff between relevance and diversity. Each point in these three plots also represents an average of 15 different locations queries. For each algorithm, we have drawn 15 points based on three super-user profiles. Thus, each super-user profile is responsible for five points, and each of these five points corresponds to a different result-set size. As cycled in red, these results have clearly shown that both

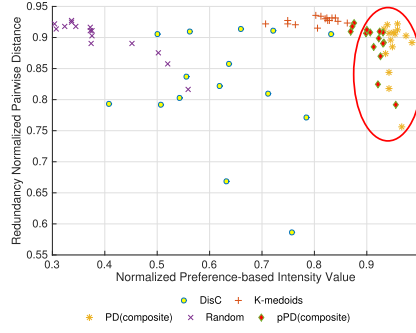


Fig. 15. Relevance vs. diversity (PIT).

our PrefDiv and pPrefDiv have delivered the best performance in terms of both relevance and diversity as the points generated by both algorithms are located on the most upper right corner of the plot.

From our empirical studies, we have observed that six of the eight tunable parameters listed in Table 2 are task-dependent parameters (i.e.,  $\lambda$ ,  $\mu$ ,  $\gamma$ ,  $\alpha$ ,  $\omega$ ,  $\xi$ ), which means that they are much more sensitive to different recommendation tasks (e.g., recommend venues/POIs, recommend movies, or recommend documents) than different users or datasets. For this reason, the provided default values for each of these six parameters in Table 2 can serve as a good starting point for any real-world venues/POIs recommendation tasks.

The other two tunable system parameters (i.e.,  $A$ ,  $\rho$ ), which are required by the PrefDiv algorithm, are user and dataset dependent. To address this issue, we are currently investigating methods to facilitate the tuning of these parameters and automatically compute the optimal value for these two parameters based on the given context [22]. These new optimizations of PrefDiv would be incorporated seamlessly into MPG as well as any other application that utilizes PrefDiv.

### 6.3 Evaluations of Route Construction

We further study the cost of incorporating serendipity through the random walk in route recommendations and evaluate the performance of different route construction schemes.

**6.3.1 Routing Schemes.** In particular, we propose four specific schemes to combine our random-walk-based routing method with our venue recommendation engines. These schemes are (i) PrefDiv+RandomWalk, (ii) pPrefDiv+RandomWalk, (iii) pPrefDiv+ShortestDistance, and (iv) pPrefDiv+HighestRelevance.

**PrefDiv+RandomWalk:** This scheme aims to incorporate serendipity in route recommendation by combining a random-walk-based non-deterministic routing method with the deterministic venue recommendation engine PrefDiv. In PrefDiv+RandomWalk, 50 random walks would be performed based on the result-set of PrefDiv to generate 50 initial routes, each of length  $K'$ . Later, one random route with the best overall performance in terms of the average composited intensity value and travel distance is selected from the Pareto Front (constructed using all 50 initial routes) as the final recommendation. Therefore, this scheme combines deterministic venues recommendation with the non-deterministic route recommendation.

**pPrefDiv+RandomWalk:** The pPrefDiv+RandomWalk scheme is similar to the previous scheme except that the non-deterministic algorithm pPrefDiv has been employed as the recommendation engine to achieve serendipity in both venue and route recommendation level. Thus, this

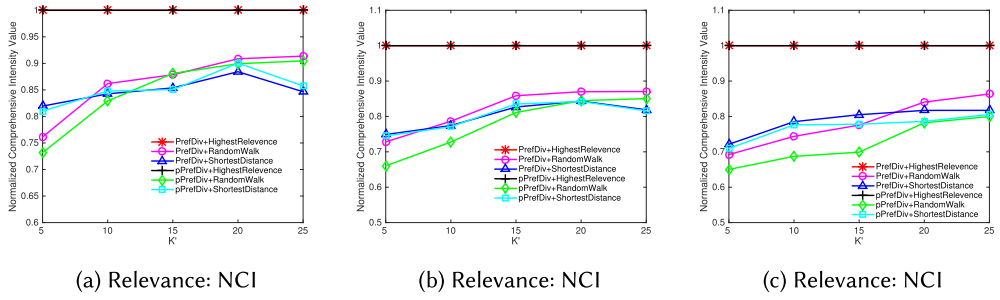


Fig. 16. Compare relevance of different routing algorithms for NYC, SF, and PIT with Super-user A.

scheme combines non-deterministic venues recommendation with the non-deterministic route recommendation.

**pPrefDiv+ShortestDistance:** For this scheme, serendipity is incorporated only in venue recommendations. As such, the shortest distance-based routing method is employed to replace the random-walk-based routing. Particularly, once the set of recommendations have been generated by pPrefDiv, the shortest route with size  $K'$  is constructed from these recommended venues, which minimize the psychical distance according to the Euclidean distance.

**pPrefDiv+HighestRelevance:** This scheme is the same as the pPrefDiv+ShortestDistance scheme, except that the route is constructed according to the ranking of the venue's average composite intensity value. Similarly to the above scheme, this scheme combines deterministic venues recommendation with the non-deterministic route recommendation.

**Baseline schemes:** To evaluate the tradeoff among relevance, travel distance, and serendipity for a given set of recommended venues  $V$ , st.  $|V| \leq k$  and a length of the route  $K'$ , st  $K' \leq K$ , we introduce two additional deterministic routing methods, (i) *highest relevance routing* and (ii) *shortest distance routing*. The former, introduced in Section 4.2, takes the given set of recommended venues and forms a route recommendation by visiting the top  $K'$  venues with the highest composite intensity value according to their ranking of composited intensity value (i.e., normalized relevance). The latter constructs the shortest travel distance route of size  $K'$  from  $V$  in a greedy fashion. Further, we combine these two routing methods with PrefDiv to form as a baseline two deterministic schemes, namely *PrefDiv+HighestRelevance* and *PrefDiv+ShortestDistance*.

**6.3.2 Evaluation Metrics.** To measure such costs, we use the *normalized relevance* (Definition 7) of all venues contained in the route, the *average similarly distance* (Definition 8) of each pair of venues in the route, and the *total physical distance* that user has to travel by following the route. As explained in Section 4.2, to capture serendipity, we use the *degree of serendipity* (Equation (12)) of each route generated by MPG.

Similarly to Section 6.2.2, we have used the average composite intensity value as a measure of Normalized Relevance and Redundancy Normalized Pairwise Distance for Average Similarity Distance.

**6.3.3 Experimental Results.** We now present the evaluation of all route recommendation schemes. Figure 16(a), (b), and (c) illustrates the average normalized composite intensity value (i.e., relevance score) of routes generated from each scheme for New York City, San Francisco, and Pittsburgh, respectively. In this set of experiments, all schemes are normalized with respect to the PrefDiv+HighestRelevance, which is the upper bound for the relevance scores. From these experiments, we observed that both random-walk- and shortest distance-based schemes perform comparably with respect to the relevance for all three cities. In addition, the serendipity-based scheme

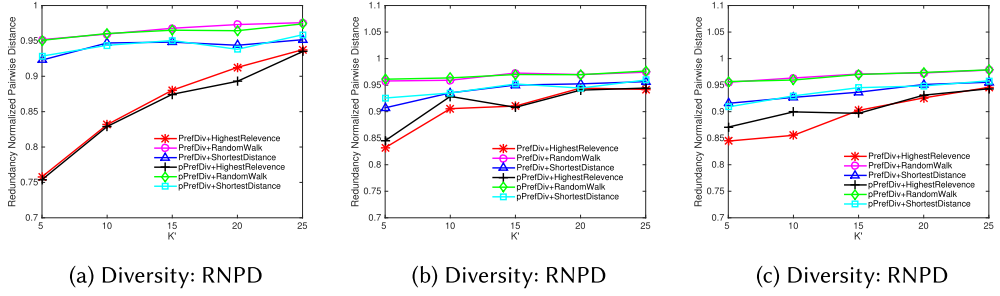


Fig. 17. Compare diversity of different routing algorithms for NYC, SF, and PIT with Super-user A.

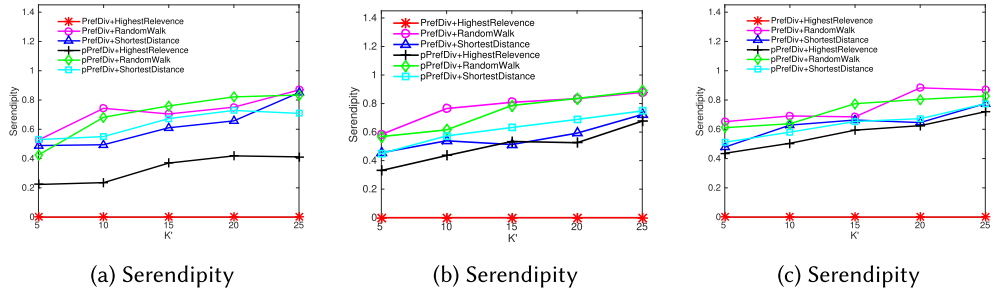


Fig. 18. Compare serendipity of different routing algorithms for NYC, SF, and PIT with Super-user A.

(i.e., PrefDiv+RandomWalk and pPrefDiv+RandomWalk) still maintained, on average, 82% of the composited intensity value when compared to the upper bound. This indicates that the serendipity introduced by employing random walk as a routing algorithm did not significantly affect the relevance of the routing. This is expected, since all schemes constructed their routes based on the highly relevant recommendations produced by our venue recommendation algorithms (i.e., PrefDiv and pPrefDiv).

Figure 17(a), (b), and (c) shows the Average Similarity Distance between each schemes. The results presented here are normalized with respect to the upper bound of the average redundancy normalized pairwise distance for each range query and result-set size involved in the experiment. From these results, PrefDiv+RandomWalk and pPrefDiv+RandomWalk demonstrate the highest performance in maintaining the diversity of the generated routes. This is due to the reason both HighestRelevance and ShortestDistance optimize toward a certain aspect of the result, such as maximizing relevance or minimizing travel distance, these optimizations often come at the price of sacrificing other contradictory aspects. However, the random walk does not suffer from this issue as it is not optimized toward any specific aspects. Among all schemes, both PrefDiv+HighestRelevance and pPrefDiv+HighestRelevance achieve the worst with respect to diversity, which is expected, since venues that are highly relevant to a user's preference have a higher chance to be semantically close venues.

Figure 18(a), (b), and (c) demonstrates the performance with respect to the serendipity for each schemes. These results indicated that the random-walk-based schemes achieved the highest serendipity. One interesting observation from these experiments is that incorporating the serendipity in either the venue recommendation or the route construction alone is still able to introduce a considerable amount of increase in the serendipity of the constructed routes. Further, incorporating the serendipity into both venue recommendation and route construction



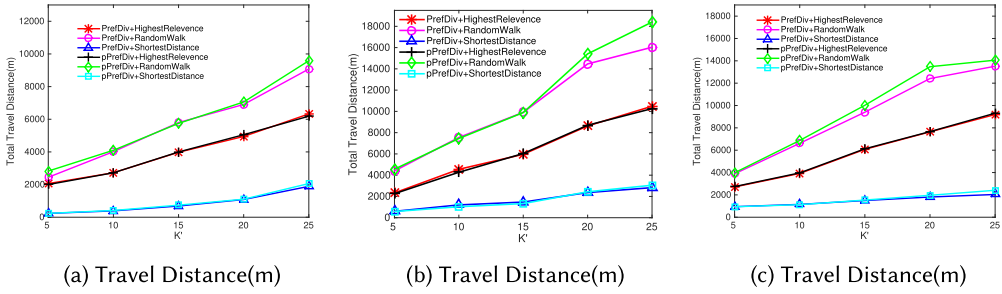


Fig. 19. Compare travel distance of different routing algorithms for NYC, SF, and PIT with Super-user A.

(i.e., through  $p$ PrefDiv+RandomWalk) does not achieve a noticeable improvement over the PrefDiv+RandomWalk. This shows that the randomness incorporated in the venue recommendation and route construction does not monotonically increase with respect to the amount of randomness of the scheme.

Figure 19(a), (b), and (c) shows the average travel distance of the routes produced by each scheme. From these figures, we observed that compared to the shortest distance-based scheme, the random-walk-based scheme does increase the travel distance. However, exploring cities with shortest routes does not necessarily indicate that something is more interesting. In fact, users may benefit more from longer travel distance when exploring a city, as it helps them to discover more places around the city. We also noticed that PrefDiv+HighestRelevance and  $p$ PrefDiv+HighestRelevance had produced routes that are shorter than random-walk-based schemes. This is due to the fact that the popularity of a venue is considered as part of its composited intensity value, as popular venues tend to be co-located with each other in a relatively small region (e.g., downtown, shopping complex, etc.), and thus reduced the total travel distance for relevance focused routing schemes.

## 7 CONCLUSIONS AND FUTURE WORK

In this article, we proposed and designed MPG, a mobile service that aims at three objectives: (i) to provide a set of diverse and surprisingly interesting venue recommendations that are better aligned with user preferences, (ii) to achieve sub-second interactive runtime in providing venue recommendations with large dataset, and (iii) to form routes within venues recommended by our proposed venue recommendation engine while still maintaining balance among *Relevance*, *Diversity*, and *Serendipity*.

We achieved our first objective through the design of MPG, which incorporates user habits, the reach willing to cover, the types of venues interested in exploring, popularity, and the diversity of venues with multiple venue recommendation engines. The second objective is achieved with the capability of  $p$ PrefDiv to efficiently produce the venue recommendations and the use of multiple optimizations (e.g., efficient query indexing structures, hashing). The third objective is achieved by proposing a set of routing schemes each targeting different objectives, setting each routing scheme as a unique combination of one venue recommendation algorithm (e.g., PrefDiv or  $p$ PrefDiv) and one routing algorithm (e.g., random walk, shortest distance) that incorporates difference levels of serendipity while preserving the relevance and diversity aspects of the routes.

To evaluate our proposed mobile service MPG, we designed the EPUI testbed, which provides user-friendly interfaces for both end-users and researchers. Our experimental evaluation through EPUI with large Foursquare datasets. Our proposed PrefDiv and  $p$ PrefDiv algorithms have enabled

sub-second interactive response time while still maintaining excellent balancing between Relevance and Diversity.

Recently, MPG and EPUI were extended to support route construction while optimizing multiple simultaneous objectives (e.g., diversity, safety, happiness, serendipity) [25]. Furthermore, the extended EPUI also serves as a testbed for exploring and evaluating venues and route recommendation solutions by enabling researchers to upload their own algorithms and compare them to well-known algorithms using different performance metrics.

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